

# Temperature of a Copper Arc

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The temperature of a copper arc in air has been measured by comparing 31 sets of transition probabilities for spectra of 20 elements with spectral-line intensities from those elements separately added to the copper. The intensities are taken from the recently published NBS Tables of Spectral-line Intensities and the transition probabilities from the literature. The individual determinations are discussed. The set of determinations is shown to follow a Gaussian distribution about a mean of 5100 °K. The average deviation of the determinations is 470 °K and the standard deviation of the mean is 110 °K. This temperature may be used in the evaluation of thousands of atomic transition probabilities from the intensities in the new tables. The effect of the uncertainty in the temperature on derived transition probabilities is evaluated as a function of excitation potential.

## 1. Introduction

Physicists have a natural interest in measuring quantities of extraordinary magnitude. This is especially true when the quantity measured permits new or more accurate evaluations of physical constants.

Such a quantity is the temperature of the electric arc in air between metallic electrodes. Well above the melting points of all materials and the boiling points of nearly all, the arc provides one of the hottest locations generally available in the physical laboratory. In such an arc it is possible to study the properties of atoms whose behavior is described by Boltzmann's law.

One particular arc, the temperature of which is especially interesting is the arc between copper electrodes, in which the spectra reported in the NBS Tables of Spectral-line Intensities were excited [1].<sup>1</sup> It happens that the temperature of this arc is susceptible of measurement by means of these very spectral-line intensity data. In itself, this would tempt us to carry out the determination; the fact that an accurate value of the temperature may enable us to evaluate transition probabilities for the 25,000 classified lines in the NBS Tables makes the temptation irresistible.

The arc has been described in the NBS Tables [1]. It was struck between two copper pellets ¼ inch in diameter, ¼ inch long, and weighing 1.5 grams each. The pellets were formed in a hydraulic press at 5000 psi from fine copper powder. Two pellets were mounted in water cooled clamps, cathode above the anode, with an arc gap of 3 mm. A direct current of 10 amperes, controlled by resistive ballast, was drawn from a 220-volt line. Exposures with which the spectra were taken varied in duration from 1 sec to 5 min depending on spectrographic efficiency and photographic plate sensitivity in different spectral regions. Separate sets of spectrograms were made for each element, using for each exposure fresh pellets to which an element had been added in the proportion of 1 atom of the element for every 1000 atoms of copper. The element was thoroughly mixed with the copper powder before pressing.

A lens at the slit of the spectrograph formed an image of the arc which fell entirely within the aperture of the grating, consequently the spectra represented radiation from all parts of the arc.

The method of temperature measurement adopted here is based on comparisons of published experimental transition probabilities of atomic lines with the intensities of the same lines measured in the copper arc. This method yields a temperature which is precisely that appropriate to the calculation of transition probabilities from our intensities.

If  $N_n$  atoms in the arc column are in an excited state  $n$ , the number of transitions per second to a lower state  $m$  will be  $N_n A_{nm}$  where  $A_{nm}$  is Einstein's probability coefficient of spontaneous emission [2]. The power from the transition is

$$I = h\nu N_n A_{nm} \quad (1)$$

where  $I$  is the intensity of the emitted line,  $h$  is Planck's constant,  $\nu$  is the frequency of the line and  $h\nu$  is the energy of a single photon. The temperature enters the comparison through its role of populating the upper level in accordance with Boltzmann's law

$$N_n = N_0 \frac{g_n}{g_0} e^{-\frac{E}{kT}} \quad (2)$$

where  $N_0$  is the population of the ground state and  $g_0$  is its statistical weight ( $2J + 1$ ),  $g_n$  is the statistical weight of the upper level,  $E$  is the energy of the upper level,  $k$  is Boltzmann's constant and  $T$  is the absolute temperature.

Substituting (2) into (1) we have

$$I = \frac{N_0}{g_0} h\nu g_n A_{nm} e^{-\frac{E}{kT}} \quad (3)$$

Substituting  $\nu = c/\lambda$ , where  $c$  is the velocity of light and  $\lambda$  the wavelength of the line, and changing into logarithmic form (base 10), (3) becomes

$$\log \frac{I\lambda}{g_n A_{nm}} = \log \frac{N_0 h c}{g_0} - \frac{0.434 E}{kT} \quad (4)$$

The first term on the right of (4) is a constant for

<sup>1</sup> Figures in brackets indicate the literature references at the end of this paper.

any particular element in this arc. We set it equal to  $C$  and solve for  $T$ . Introducing a value for  $k$ ,

$$T = - \frac{625E}{\log \frac{I\lambda}{gA} - C} \quad (5)$$

where  $T$  is in  $^{\circ}\text{K}$ ,  $gA = g_n A_{nm}$  and  $E$  is in units of  $10^3 \text{ cm}^{-1}$  which we will call kilokaysers ( $1 \text{ kK} = 1000 \text{ cm}^{-1}$ ) in accordance with a suggestion of Meggers [3]. The value of  $T$  is most conveniently obtained from a plot of  $\log I\lambda/gA$  versus  $E$  for each spectrum in which relative values of  $gA$  are known. The constant  $C$  does not affect the slope of the line from which  $T$  is determined.

The ordinate is equivalent to  $\log N_n/g_n$  so the plot is in effect a display of the population of excited levels in the atom as a function of the level value. Plots for eight sets of transition probabilities taken from the literature and compared with our intensities are given in figures 1 to 8. The straightness of the plots clearly shows that the observations are in accord with the Boltzmann distribution. The population of levels of equal statistical weight declines exponentially with increasing energy values.

If the  $f$ -value is known instead of  $A$ , we may use Ladenburg's [4] equation

$$g_n A_{nm} = \frac{8\pi^2 e^2}{mc} \frac{g_m f_{mn}}{\lambda^2} \quad (6)$$

for converting eq (5) to the form

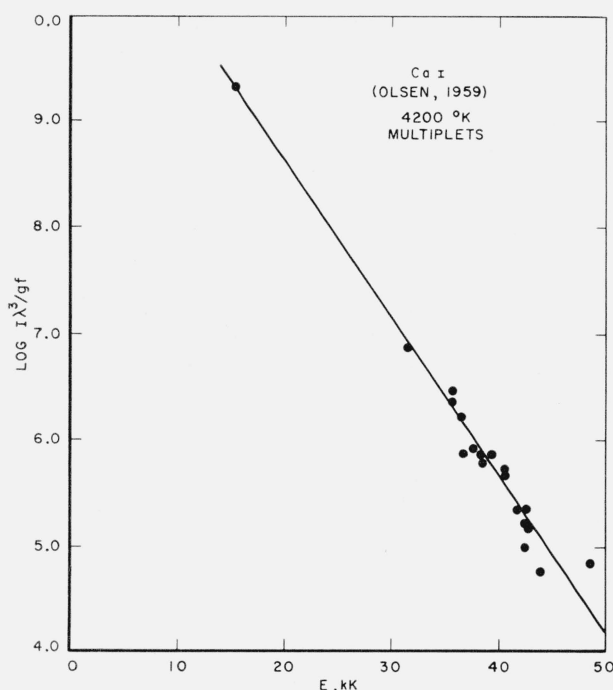


FIGURE 1. Log ratio of intensity  $\times \lambda^3$  to  $gf$ -value for multiplets of Ca I in the copper arc plotted versus upper level.

An arc temperature of 4200  $^{\circ}\text{K}$  is derived from the slope of the line of best fit.

$$T = \frac{-625E}{\log \frac{I\lambda^3}{gf} - C'} \quad (7)$$

where  $gf = g_m f_{mn} (= g_n f_{nm})$ , and  $C'$  is a constant.

We assume that the temperature of the arc was constant during the exposure of each of the hundreds of spectrograms in which our intensity observations were made. Great care was taken in the preparation of the electrodes and in the operation of the arc to insure uniformity in the experimental conditions from exposure to exposure. The NBS intensity data used in the 31 temperature determinations reported in section 4 of this paper are taken from about 50 separate exposures. It will be shown in the discussion that the variation in the determinations arises, at least in part, from systematic errors amongst the sets of transition probabilities.

## 2. Excitation in the Arc in Air at Atmospheric Pressure

The question arises whether we should be able to assign a valid temperature which can be used to describe the intensity of spectral lines emitted in accordance with eq (3). If there are several processes of excitation at work, each operating at a different effective temperature, then eq (3) is not valid. In a classical investigation, Ornstein and Brinkman [5] have shown that excitation in the column of the ordinary arc in air is controlled by collisions between atoms and molecules in a strictly thermal fashion. The same process is responsible for ionization and dissociation. They found that the excitation was well described by Boltzmann's law and that ionization followed Saha's equation, which also demands a thermal aggregation of particles. Experiments by Elenbaas described by Cobine [6] show that in arcs at pressures above 20 mm Hg, the electron and gas

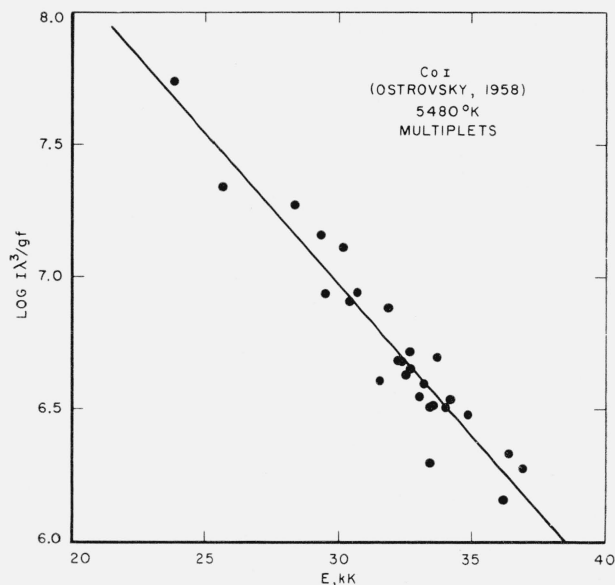


FIGURE 2. Log ratio of intensity  $\times \lambda^3$  to  $gf$ -value for multiplets of Co I in the copper arc plotted versus upper level.

An arc temperature of 5480  $^{\circ}\text{K}$  is derived from the slope of the line of best fit

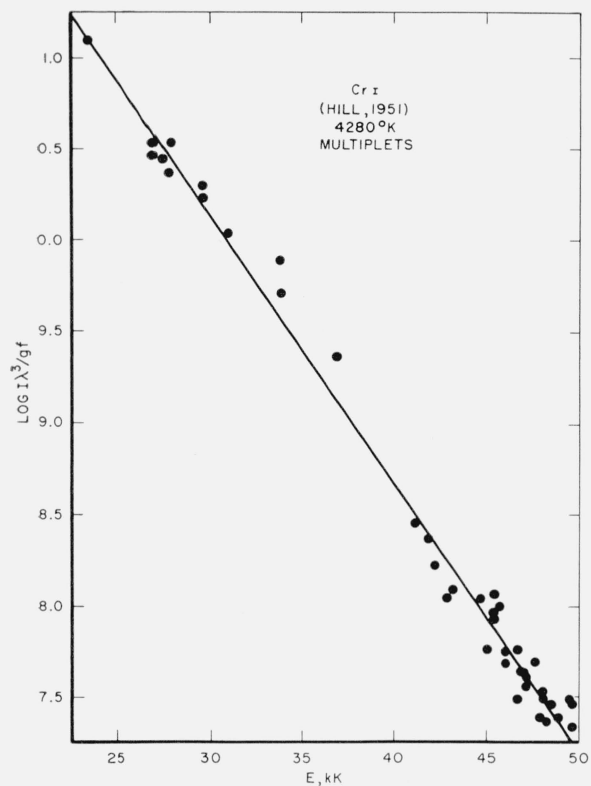


FIGURE 3. *Log ratio of intensity  $\times \lambda^3$  to gf-value for multiplets of Cr I in the copper arc plotted versus upper level.*

An arc temperature of 4280 °K is derived from the slope of the line of best fit.

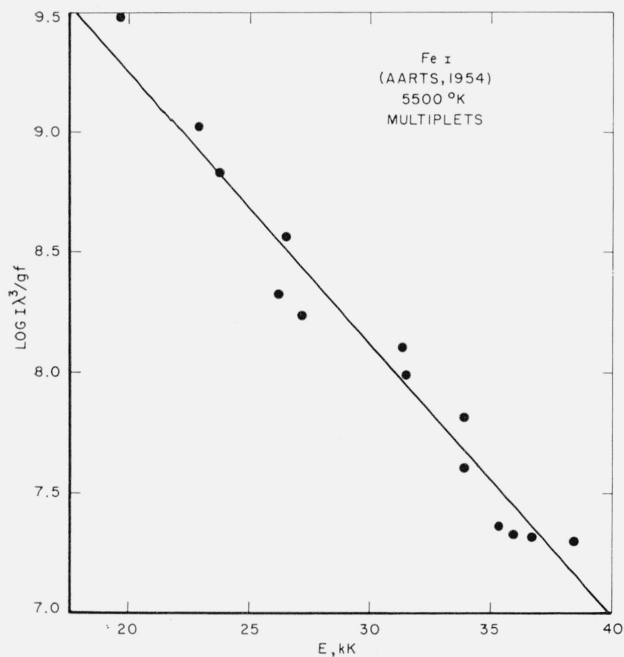


FIGURE 4. *Log ratio of intensity  $\times \lambda^3$  to gf-value for multiplets of Fe I in the copper arc plotted versus upper level.*

An arc temperature of 5500 °K is derived from the slope of the line of best fit.

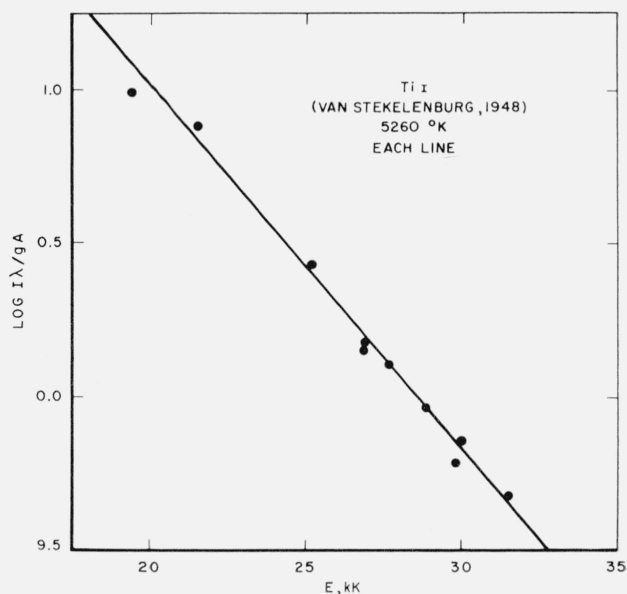


FIGURE 5. *Log ratio of intensity  $\times \lambda$  to gf-value for lines of Ti I in the copper arc plotted versus upper level.*

An arc temperature of 5260 °K is derived from the slope of the line of best fit.

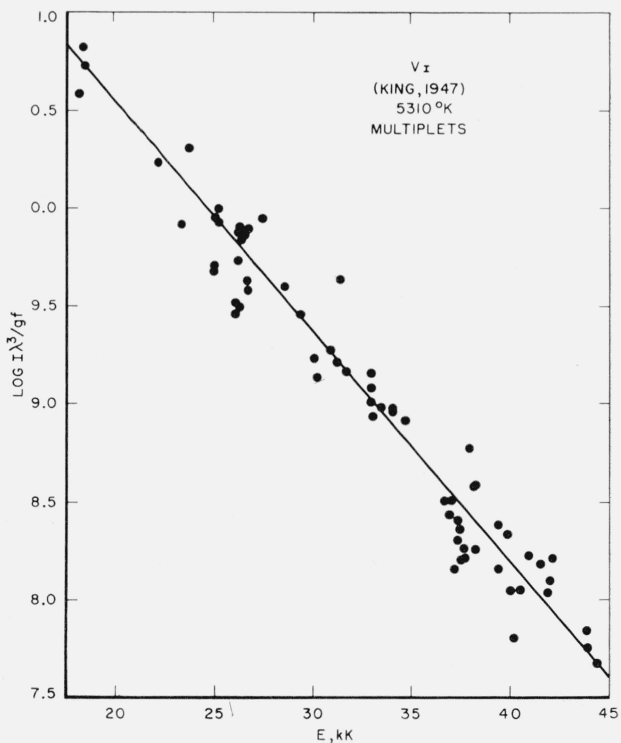


FIGURE 6. *Log ratio of intensity  $\times \lambda^3$  to gf-value for multiplets of V I in the copper arc plotted versus upper level.*

An arc temperature of 5310 °K is derived from the slope of the line of best fit.

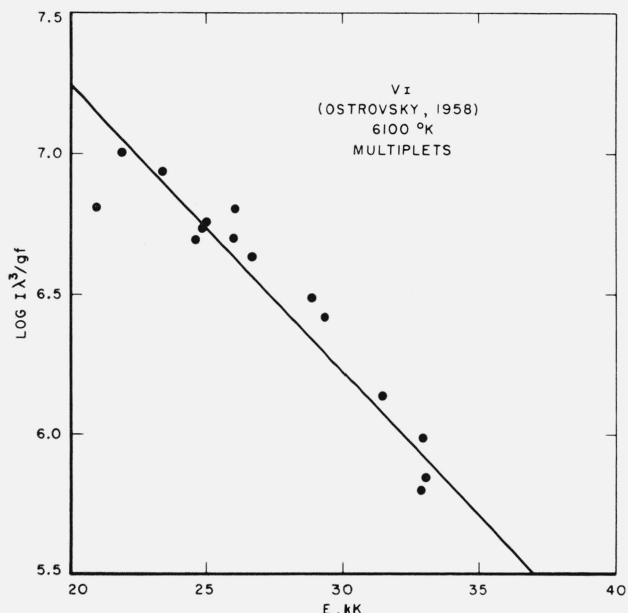


FIGURE 7. *Log ratio of intensity  $\times \lambda^3$  to  $gf$ -value for multiplets of V I in the copper arc plotted versus upper level.*

An arc temperature of 6100 °K is derived from the slope of the line of best fit.

temperatures are equal. Suits [7] has measured the gas temperature and positive ion temperature in arcs at atmospheric pressure and found them equal within an experimental error of 300 °K.

The investigations quoted above are of interest in considering excitation in arcs. However, in this investigation we need not depend on them. The remainder of this paper is devoted to a discussion of graphical evaluations of temperature from eq (5) or (6), using 31 sets of transition probabilities taken from the literature. Examples are shown in figures 1 through 8. The linearity of these plots establishes beyond doubt that the excitation in our arc is described by Boltzmann's law. The fact that the excitation does follow Boltzmann's law enables us to calculate transition probabilities from intensities and conversely. The question of the existence of complete thermodynamical equilibrium per se becomes irrelevant for our purpose.

### 3. Choice of Transition Probabilities

The values of relative transition probabilities available for comparison with our intensities may be divided into four categories: (1) Experimental values based on independent temperature determinations; (2) experimental values based on temperature determinations obtained with data from category (1); (3) values calculated by quantum-mechanical methods (e.g., Hartree-Fock); and (4) values calculated with the approximate theory of Bates and Damgaard. Several trials with data from categories (3) and (4) resulted in plots of eq (7) exhibiting such a large scatter of points that no reasonably reliable temperature could be derived. Allen [8], in a similar investigation, states that use of Bates and Damgaard

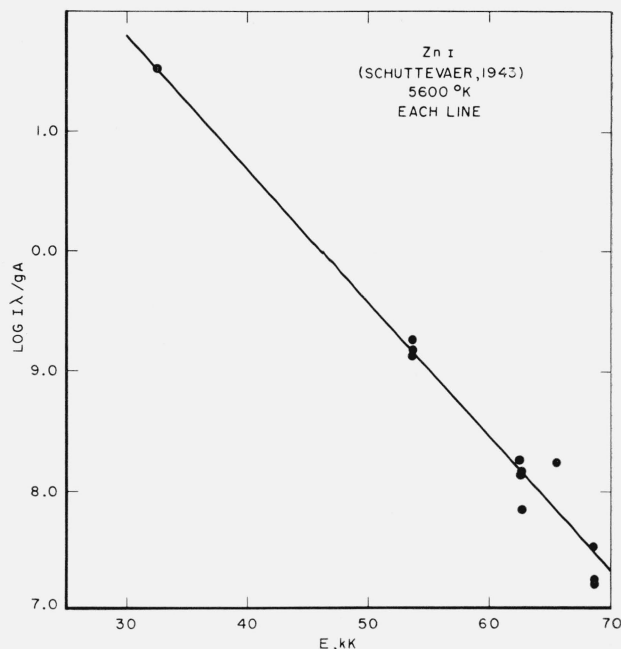


FIGURE 8. *Log ratio of intensity  $\times \lambda$  to  $gA$  for lines of Zn I in the copper arc plotted versus upper level.*

An arc temperature of 5600 °K is derived from the slope of the line of best fit.

values leads to impossibly high arc temperatures, particularly in complex spectra. Category (2) is obviously inadmissible for our purposes, since such a set of data would merely duplicate the information from category (1) with which it was calibrated.

We are left with the experimental data of category (1) for our temperature determination. These data are reviewed up to 1954 by R. B. King [9] who noted about 2000 known values. The number has since increased to about 2200.

### 4. Results

A rather complete search of the published literature on experimental transition probabilities disclosed 31 sets of data suitable for comparison with the intensities in the NBS Tables. All independent sets of data with more than 4 lines in common with those of our tables (and from which temperatures could be derived) were included, with one exception discussed in section 5. The results are summarized in table 1. Column 1 gives the spectrum investigated by the authors in col. 2. The data came from 5 laboratories, indicated in col. 3, and listed below.

Physical Institute of the State University at Leningrad.....	11 sets
Physical Laboratory of the University of Utrecht.....	10 sets
Norman Bridge Laboratory of the Cali- fornia Institute of Technology.....	7 sets
Physical Institute, Academy of Sciences USSR, Moscow.....	2 sets
Zeeman Laboratory at the University of Amsterdam.....	1 set



TABLE 1. Individual determinations of copper arc temperature

Spectrum	Author	Laboratory	Date	Ref.	Method	No. of lines	Range of E	$\Delta E$	T	Dev.
Ag I	Terpstra et al.	Utrecht	1958	[10]	Arc	8	kK	kK	°K	°K
Ba I	Kruthof	Utrecht	1943	[11]	Arc	10	43-54	11	4600	500
Ba I	Ostrovsky et al.	Leningrad	1960	[12]	Hook	54	26-35	9	4250	850
Ca I	Schuttevaer et al.	Utrecht	1943	[13]	Arc	12	13-36	23	5000	100
Ca I	Olsen et al.	California	1959	[14]	Furn. abs.	63	32-43	11	4880	220
Cd I	Hengstum et al.	Utrecht	1956	[15]	Arc	15	15-49	34	4200	900
Cd I	Penkin et al.	Leningrad	1960	[16]	Hook and em.	13	51-65	14	5080	20
Co I	King et al.	California	1955	[17]	Furn. abs.	181	24-46	22	4750	350
Co I	Ostrovsky et al.	Leningrad	1958	[18]	Hook	79	24-37	13	5380	280
Cr I	Hill et al.	California	1951	[19]	Furn. abs.	137	24-50	26	5480	380
Fe I	(King et al.	California	1938	[20]	Furn. abs.	180	19-52	33	4820	280
	Carter	California	1949	[21]	Furn. em.					
Fe I	Sobolev (table 3)	Moscow	1943	[22]	Arc	15	33-46	13	4850	250
Fe I	Sobolev (table 5)	Moscow	1943	[22]	Arc	32	27-40	13	5320	220
Fe I	Aarts et al.	Amsterdam	1954	[23]	Furn. em.	59	20-38	18	5500	400
Ga I	Ostrovsky et al.	Leningrad	1958	[24]	Hook	5	25-35	10	5750	650
Hg I	Schouten et al.	Utrecht	1943	[25]	Arc	8	62-71	9	6250	1150
In I	Ostrovsky et al.	Leningrad	1958	[24]	Hook	5	24-33	9	4510	590
K I	van der Held et al.	Utrecht	1936	[26]	Flame	6	13-27	14	5100	0
Mg I	Kersten et al.	Utrecht	1941	[27]	Arc	18	41-58	17	5780	680
Mn I	Ostrovsky et al.	Leningrad	1957	[28]	Hook	9	18-36	18	3900	1200
Ni I	King	California	1948	[29]	Furn. abs.	89	28-37	9	4660	440
Se I	Ostrovsky et al.	Leningrad	1957	[30]	Hook	33	16-33	17	5100	0
Sr I	Schuttevaer et al.	Utrecht	1943	[13]	Arc	8	15-40	25	4410	690
Tl I	King et al.	California	1938	[20]	Furn. abs.	204	19-40	21	5080	20
Tl I	van Stekelenburg et al.	Utrecht	1948	[31]	Arc	28	19-32	13	5260	160
Tl I	Ostrovsky et al.	Leningrad	1956	[32]	Hook	56	19-34	15	5400	300
Tl I	Filippov et al.	Leningrad	1933	[33]	Hook	5	26-43	17	6400	1300
V I	King	California	1947	[34]	Furn. abs.	224	18-42	24	5310	210
V I	Ostrovsky	Leningrad	1958	[18]	Hook	78	21-33	12	6100	1000
Zn I	Schuttevaer et al.	Utrecht	1943	[35]	Arc	12	31-69	38	5600	500
Zn I	Penkin et al.	Leningrad	1960	[16]	Hook and em.	12	54-68	14	5160	60

The date of publication is given in col. 4 and the reference number, as listed at the end of this paper, in col. 5. The method used in the paper is indicated in col. 6. In general, the several laboratories use different methods. At Leningrad the anomalous dispersion of the vapor in the neighborhood of the absorption lines from a furnace is employed according to the "hook" method of Rogestwensky [36], sometimes with variations. The temperature of the tube furnace is measured with an optical pyrometer. At Utrecht measurements are made usually with the arc method originated by Ornstein and his co-workers [5] and carried on by Professor Smit [37]. In that procedure, the temperature is usually measured from the intensity distribution in the CN bands in the spectrum. The California experiments generally follow the method of total absorption as developed by King and King [38]. The furnace temperature is measured with an optical pyrometer.

The number of spectral lines utilized in each determination is given in col. 7. The largest numbers are from California. The minimum and maximum values of upper excitation potential and the differences between them are given in cols. 8 and 9. These determine the range of the abscissae of the plots and thus affect to some extent the precision of the slope determination. The temperature determined from the slope of the plot appears in col. 10 and its deviation from the mean value in col. 11. The average value of the 31 individual determinations is 5100 °K and the average deviation is 470 °K (9%). The standard deviation of an individual determination, which is a measure of the scatter of the determinations, is given by

$$\sigma = \sqrt{\frac{\sum \text{dev.}^2}{n-1}}$$

and is equal to 600 °K (12%). The standard deviation of the mean, which measures the precision of the result, is given by

$$\sigma_m = \sqrt{\frac{\sum \text{dev.}^2}{n(n-1)}}$$

and is equal to 110 °K (2%). The median value is also 5100 °K.

It is of interest to compare the results from the three major contributors of transition probability data. This is done in table 2. The three mean values agree amongst themselves within their uncertainties. Another test of the data was made by selecting 12 sets of data which, on the basis of small scatter and uniform distribution of the points, and adequate range of  $E$ , seemed to give promise of better determinations. The average of these 12 is 5000 °K with an average deviation of 500 °K. These values are not significantly different from the general averages. The above mentioned tests provide some confidence in the adoption of an unweighted mean as the best value for the temperature.

Eight of the plots from which the temperatures were derived are reproduced in the figures. In each figure is given the spectrum, the reference from which the transition probabilities were taken, the temperature derived from the plot and a note whether each point on the plot represents a single spectral line or the average value for a multiplet.

TABLE 2. Comparison of laboratories

Spectrum	Temp.	Dev.
California		
Ca I	4200	620
Cr I	4280	540
Ni I	4660	240
Fe I	4820	0
Ti I	5080	260
V I	5310	490
Co I	5380	560
Avg	4820	390
$\sigma = 470$		
Leningrad		
Mn I	3900	1330
In I	4510	720
Cd I	4750	480
Ba I	5000	230
Sc I	5100	130
Zn I	5160	70
Ti I	5400	170
Co I	5480	250
Ga I	5780	520
V I	6100	870
Tl I	6400	1170
Avg	5230	540
$\sigma = 720$		
Utrecht		
Ba I	4250	870
Sr I	4410	710
Ag I	4600	520
Ca I	4880	240
Cd I	5080	40
K I	5100	0
Ti I	5260	140
Zn I	5600	480
Mg I	5780	660
Hg I	6250	1130
Avg	5120	480
$\sigma = 630$		

## 5. Discussion of Results

It might not be amiss to discuss briefly the individual determinations. Ag gave a good plot, but with only a small range of  $E$  and a small number of lines. The Leningrad Ba data are excellent, except for low values of  $gf$  for 4132 and 3889 Å which were probably caused by the proximity of strong lines at 4130 and 3891 Å. The Utrecht Ba plot is good. Both plots of Cd are good and they agree well. Both Ca plots are excellent; the California one covers an unusually long range of  $E$  (see fig. 1). The plot of the Co data from California is long and straight but shows some scatter; the Leningrad one is shorter but with less scatter (see fig. 2). The low temperature which is obtained with the California Cr data has been noticed by several other people and is discussed by Goldberg, Muller, and Aller [39]. Otherwise a good plot is obtained (fig. 3). A set of Cr data from Leningrad shows such a large scatter and small range of  $E$  that no temperature could be derived [28].

In the California Fe plot, all the lines below 3200 Å stand above the line. These were ignored in deriving the slope. The Moscow Fe data show a rather large scatter but yield satisfactory temperatures. The same paper [22] gives a set of data for Bi, which, although apparently in good order, yields a temperature of 8700 °K, which differs from the general mean by six times the standard deviation and it has been rejected, as noted above. The Amsterdam Fe data form an excellent plot with a good range of  $E$  and a small scatter (see fig. 4).

The Ga and In data are deficient in number and involve only resonance lines which are generally subject to various experimental difficulties, but they give a satisfactory plot. The plot for Hg covers too short a range of  $E$  because the NBS intensity of the resonance line was affected by self-absorption and could not be used. K represents the only data obtained from flames, and, although necessarily deficient in number of lines, yields a satisfactory plot. It involves the resonance lines, which showed no self-absorption in the NBS spectra. The Mg data show a good distribution and a very small scatter. The Mg resonance line was omitted because of self-absorption in the NBS line. The Mn resonance lines fall high on the Mn plot, indicating too low a value of  $gf$  from the hook method, and they were not used in finding the slope. Ni gives a good plot but with a small range of  $E$ . As in the case of Mn, the resonance lines of Sc are high on the plot and were ignored in determining the slope. The hook method apparently tends to give low values for the strongest lines. The Utrecht Sr data make a nice plot over a good range of  $E$ . Another set of Sr data obtained by Eberhagen at Göttingen [40] by using the Kiel water-arc forms a set of points with too large a scatter to permit a determination of temperature.

Data for Ti are available from three laboratories. The California set has a large number of points well distributed over a long range of  $E$  and a very small scatter. A preliminary plot of these data is shown in ref. [1]. The Utrecht data are fewer and have a smaller range, but shown almost no scatter. The maximum vertical deviation of a point from the best line is 0.09 log units which represents a maximum deviation of 23 percent (see fig. 5). The Leningrad data have more points but a considerable scatter. It may be mentioned at this point that Miss Rountree [41] has calculated a temperature for our arc from our Ti data and King's. Her value is slightly high because she omitted the  $\lambda^3$  factor of eq (7). The Tl data from Leningrad have been frequently cited in the Russian literature. There are only 5 lines in common with ours. The fact that the temperature derived from these data shows the maximum deviation in the group of 31 values may arise from the location of 4 of the 5 lines in the short wavelength regions below 2800 Å where the accuracy of the intensities declines. The V data from California have the largest number of lines in the group and the plot shows a moderate scatter of points well distributed over a long range of  $E$ , permitting an accurate determination of  $T$ . It shows no suggestion of curvature, indicating strict adherence to Boltz-

mann's law (see fig. 6). The Leningrad data cover a shorter range of  $E$  (see fig. 7). The Utrecht data for Zn cover the longest range of  $E$  of the whole group and give a very straight plot (see fig. 8). The Leningrad data omit the intersystem line at 3075 Å and so have a more restricted range of  $E$ .

Taken as a whole, the results exhibit a nearly normal (Gaussian) distribution of values (see table 3). Consideration of the results in table 1 suggests that the effective temperature of the copper arc is substantially constant and that the variations arise from systematic errors in the various sets of transition probabilities. For example, the two sets of  $gf$ -values for V I exhibited in figures 6 and 7 are compared with the same intensity numbers in each case. The temperature difference of 780 °K between the values from each plot can arise only from systematic errors inherent in the two sets of  $gf$ -values. Similarly, the transition probabilities of van Hengstum and Smit [15] for Cd I are systematically smaller relative to those of Penkin and Redko [16] at the larger values of  $E$ , so although the identical NBS intensity numbers are used, the two plots yield temperatures which differ by 330 °K. The diversity of methods represented and the independent nature of the laboratories leads us to suppose that these systematic errors have offset one another to some extent in contributing to the general average value.

Various correlation plots have been made to determine other systematic influences on the derived temperatures. There appears to be no correlation with the number of lines used, with atomic number, with range of  $E$  (abscissae of the plots), with magnitude of  $E$ , nor with ionization potential.

TABLE 3. *Distribution of individual temperature determinations about the mean, in intervals of  $\sigma$ .*

Interval.....	3300- 3900	3900- 4500	4500- 5100	5100- 5700	5700- 6300	6300- 6900
Individual determinations	3900	4200 4250 4280 4410	4510 4600 4660 4750 4820 4850 4880 5000 5080 5080 5100	5100 5160 5260 5310 5320 5380 5400 5480 5500 5600	5750 5780 6100 6250	6400
Observed fraction.....	0.03	0.13	0.36	0.32	0.13	0.03
Expected (Gaussian)....	.02	.14	.34	.34	.14	.02

## 6. Effect of Uncertainty in Temperature on Uncertainty in Derived Transition Probability

The purpose of determining the best value of the temperature of the copper arc is to enable us to calculate values of  $gA$  or  $gf$  from the intensities of the classified lines in the NBS Tables of Spectral-line Intensities. We must find out how the uncertainty of the value of  $T$  will influence the uncertainty of the  $gA$  or  $gf$ .

If we differentiate eq (3) with respect to  $T$  and divide the result by eq (3) we have

$$\frac{d(gA)}{gA} = -\frac{E}{kT} \frac{dT}{T}.$$

Introducing numerical values we find

$$\frac{d(gA)}{gA} = -\frac{E}{3.54 T} \frac{dT}{T}.$$

Now if  $\frac{dT}{T}$  is 2 percent, then

$$\frac{d(gA)}{gA} = -0.00565 E.$$

Similarly

$$\frac{d(gf)}{gf} = -0.00565 E.$$

The magnitude of the error for values of the upper level from 10 to 100 kilokaysers is given in table 4, assuming a temperature of 5100 °K and an uncertainty in the temperature of 2 percent. Most of the lines in the NBS tables have upper levels less than 50 kK, so most of the errors introduced by the temperature error will be less than 30 percent. This is about the same as the errors in the intensity numbers themselves.

TABLE 4. *Error in  $gf$  of  $gA$  corresponding to a 2 percent error in  $T$  at 5100 °K*

$E$ in kK	% error in $gf$ or $gA$
10	6
20	11
30	17
40	23
50	28
60	34
70	40
80	45
90	51
100	56

## 7. Conclusion

A temperature for the copper arc in which the intensities published in the NBS Tables of Spectral-line Intensities [1] were measured has been determined. Comparison of NBS intensities with 1650 published transition probabilities for 20 different spectra yields the value

$$5100 \pm 110 \text{ °K.}$$

With this parameter, relative transition probabilities for the 25,000 classified lines in the NBS Tables can be computed.

Further studies are in progress to determine the state of ionization of each element in the arc. This will allow the relative values for each spectrum to be adjusted to the same scale. It may then be possible to calibrate the scale on an absolute basis as Allen

has done [42]. All the pertinent data for the 25,000 lines are on punched cards and the computation can be performed very quickly, once the proper parameters and factors have been determined.

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